

Studying the emergence of invasiveness in tumours using game theory

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Abstract. Tumour cells have to acquire a number of capabilities if a neoplasm is to become a cancer. One of these key capabilities is increased motility which is needed for invasion of other tissues and metastasis. This paper presents a qualitative mathematical model based on game theory and computer simulations using cellular automata. With this model we study the circumstances under which mutations that confer increased motility to cells can spread through a tumour made of rapidly proliferating cells. The analysis suggests therapies that could help prevent the progression towards malignancy and invasiveness of benign tumours.

PACS. 87.17.Aa Modeling, computer simulation of cell processes – 87.19.xj Cancer – 87.23.Kg Dynamics of evolution

1 Introduction

Carcinogenesis is the process that describes the transformation of healthy cells into cancer cells. Cancer has long been recognised as an evolutionary disease [1]. It is also a disease in which the environment (other cells in the tissue, nutrients, pH, etc.) determines which genetic mutations lead to phenotypes that spread through the population. Hanahan and Weinberg [2] have described six capabilities that tumour cells have to acquire during carcinogenesis for a tumour to become a cancer, that is, a tumour capable of invasion and metastasis. These capabilities include: unlimited replicative potential, environmental independence for growth, evasion of apoptosis, angiogenesis and invasion. This paper focuses on how a tumour made of rapidly proliferating cells acquires invasiveness with some of the cells becoming capable of motility. We call proliferative cells those cells that do not rely on the environment for growth, which in many cases involves mutations in genes such as APC, K-RAS and TGF. The motile cells are those tumour cells that, through abnormal regulation of the synthesis of cadherins and integrins, have an increase in their motility and invasiveness compared to other cell types [3,4]. This transition is a prerequisite for invasion and is key in the progression of a tumour towards malignancy.

Tumours are the result of somatic evolution: the mutations that promote tumour initiation lead to an ecosystem in which different tumour cell phenotypes compete for space and resources [5]. Evolutionary game theory is an appropriate modelling tool in which to frame tumouri-

genesis [6] and in which to study the possible equilibria between two or more phenotypes under different microenvironmental circumstances. In this paper we also describe an agent-based model using a cellular automaton. This alternative model, in which the agents can be either proliferative or motile tumour cells, has been designed to mirror, as closely as possible, the game theoretical model but whereas the first model is suitable for analysis, the simulations provided by the second have been used to study the influence of space on the results. Both models show that abundance of resources reduces the likelihood of success of motile cells. They also show that typically, there will be many circumstances that could lead to polyclonal tumours that would include both: proliferative and motile cells.

2 Previous studies

Game theory (GT), first formalised by von Neumann and Morgenstern [7], has a long tradition in the field of economy [8]. It has also been successfully applied to evolutionary biology [9,10]. Its use in the field of theoretical medicine is much more recent although its future looks quite promising [6]. GT is a powerful tool when studying the interactions between a number of entities called players in which the fitness of each player depends not only on what the player decides to do (its strategy) but also on what the other players do. In evolutionary GT the strategy of an individual is an aspect of its phenotype that affects its behaviour in the game. One important concept in evolutionary game theory is that of an evolutionary stable

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strategy (ESS). A strategy is ESS if, when adopted by a population, it cannot be successfully invaded by an alternative strategy as a result of evolution. An overview of the application of GT in cancer research can be found in [11]. The first use of GT in the field of cancer research was described by Tomlinson and Bodmer [12,13]. Their models are based on pairwise interactions between different types of tumour cell phenotypes in the context of several cancer related problems such as angiogenesis, evasion of apoptosis or the production of cytotoxic factors. In these problems, game theory is employed to analyse the circumstances that lead to polymorphism that is, coexistence of two phenotypes. Subsequent research carried out by Bach and colleagues extended this idea to interactions between three players in the angiogenesis problem [14] and also studied the effect of spatial dynamics on the equilibria [15]. Gatenby and Vincent adopted a game theory approach heavily influenced by population dynamics to investigate the influence of the tumour-host interface in colorectal carcinogenesis [16,17] and suggest therapeutic strategies [18]. More recently Mansury and colleagues [19] have produced a modified game theory approach in which they study how the interactions between two types of phenotypes, proliferative and motile, in a tumour affect a number of features of the tumour growth dynamics. This model does not contemplate evolutionary dynamics and thus cannot address questions related to the effect of model parameters on the coexistence of different phenotypes in a polymorphic tumour. Recently, Axelrod and colleagues have suggested, although never demonstrated, how GT could be used to study the possible cooperation of different tumour sub-populations during tumour progression [20,21].

Cellular automata (CA) are another invention of von Neumann [22] who, together with Stanislaw Ulam, created them to study self replication. CA are based on the concepts of discrete space and time and are well suited to model processes at the cellular level [23]. CA have been extensively used to model many aspects relevant in cancer research [24,25] such as early tumour growth [19,26], invasion [27–30], angiogenesis [31,32] and evolution [33,34].

3 The game theory model

The model assumes a very simple microenvironment inhabited initially only by proliferative cells mimicking the situation in many benign tumours [1]. The motile phenotype can appear as a result of one or more genetic mutations. The interactions between these two phenotypes are characterised in Table 1. Parameter b is the base payoff that corresponds to a cell that does not need to share resources (glucose, oxygen, etc.) with any one else. The cost of motility c represents the fitness loss incurred by any motile cell that at a given moment chooses to move to a neighbouring location. This cost could represent for instance the fact that cells that are capable of motility cannot divide while moving [35,36]. When a motile cell finds a proliferative cell then the proliferative cell stays and uses all the resources of that location. The motile cell moves to a different location where it is assumed that it

Table 1. Payoff table that represents the change in fitness of a tumour cell with a given phenotype interacting with another cell. The base payoff in a given interaction is b and the cost of moving to another location with respect to the base payoff is c .

	Proliferative	Motile
Proliferative	$\frac{1}{2}$	$b - c$
Motile	b	$b - \frac{c}{2}$

will find a similar amount of resources. When two motile cells meet then one of them stays and takes the resources whereas the other moves to another location. When two proliferative cells interact they have to share the resources of the location in which they find themselves. Given the payoffs shown in Table 1, the Bishop-Cannings theorem [9] can be used to obtain the mixed strategy that would be an evolutionary stable strategy (ESS). A mixed strategy is a strategy in which one of a number of pure strategies can be used with a given probability. If the pure strategies are to be motile or to be proliferative then a mixed strategy could be 0.6 implying that the cell would play the strategy of motility with probability 0.6 and the strategy proliferative with 0.4. A mixed strategy in this game could also correspond to a population composed of more than one phenotype.

The genetic polymorphism, in which the two phenotypes coexist in the tumour, can be calculated if we assume that for an equilibrium to exist, the payoff of one strategy is equal to the payoff of the other strategy, thus $pE(m, m) + (1 - p)E(m, p) = pE(p, m) + (1 - p)E(p, p)$, where p is the probability of a cell having the motile phenotype and $E(x, y)$ is the payoff for a cell with phenotype x when meeting a cell with phenotype y . The values of E can be extracted from Table 1 and thus, the probability p of adopting strategy motility in equilibrium varies with b and c (with c not more than half the base payoff) as shown in the following equation:

$$p = \frac{b - 2c}{b - c}. \quad (1)$$

Figure 1 shows the proportion of motile phenotypes in the population when the base payoff, b , is fixed. It can be proven that in games with only two pure strategies there is always one stable mixed strategy and the composition of pure strategies in it corresponds to a polymorphism [9].

4 The cellular automaton model

The GT model does not take into account the influence of space in the dynamics of tumour evolution. For that reason we have introduced a cellular automaton (CA) with the aim of producing a spatial model in which the behaviour of proliferative and motile cells can be investigated. Space in the CA is characterised by a 1000×1000 lattice in which each site can host one or more tumour cells. The carrying capacity of a lattice site corresponds to the area in which one cell can affect another one. Each

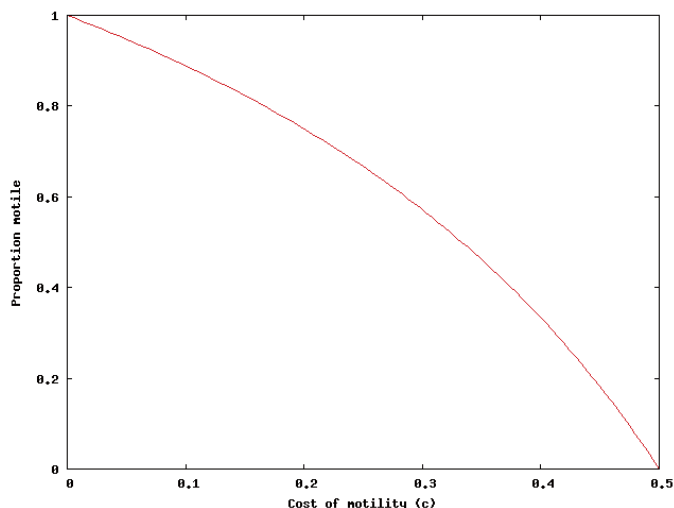


Fig. 1. The graph shows the results of analysing the game theoretical model. The X-axis shows the value of the cost of motility and the Y-axis shows the proportion of the population with the motile phenotype.

1 lattice site also contains nutrients which are needed for cell
 2 proliferation. Nutrients are assumed to be homogeneously
 3 distributed in the lattice and replenished to a given constant
 4 value each time step. Thus the resources that determine cell
 5 proliferation are available space and nutrients. Cells interact
 6 and share resources only with other cells in the same lattice
 7 site. This very simple microenvironment mimics the one that
 8 is implicitly assumed in the GT model. The behaviour of the
 9 tumour cell types was designed to resemble, as closely as possible,
 10 that of the two phenotypes of the GT model. It features proliferative
 11 and motile cells. The former do not move even if that means
 12 sharing an ever decreasing amount of resources. The latter
 13 divide only when they do not have to share the available
 14 resources with no other cell and try to move to a better
 15 location otherwise. The precise behaviour of the different
 16 phenotypes is the following. The cells with the proliferative
 17 phenotype divide if there are enough nutrients in the
 18 lattice site. The new offspring will be created in the same
 19 site as the progenitor unless the population of cells at that
 20 site has exceeded the maximum carrying capacity. In the
 21 last case the offspring is created in a neighbouring location
 22 having the lowest density of cells (see Fig. 2). Motile
 23 cells will never share a lattice site with another cell if there
 24 is more available space in a neighbouring location. Thus,
 25 motile cells always move to a neighbouring site if the density
 26 of the new location is lower than that of the current
 27 location. If more than one neighbouring location is equally
 28 suitable then the new location will be selected randomly
 29 among them. On the other hand if the location is suitable
 30 and there are enough nutrients then the cell will produce
 31 offspring in the same location as the parent (see Fig. 3).

The update of the CA is as follows:

- 34 – If cell is motile and there are neighbours:
- 35 – look for the neighbouring lattice site with the
- 36 smallest cell count;

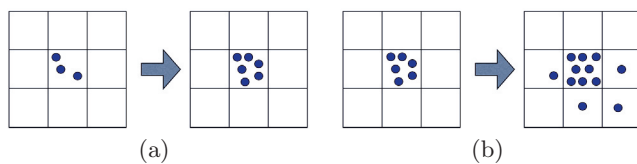


Fig. 2. Behaviour of proliferative cells. (a) In the example each lattice site can host up to 8 tumour cells. When the lattice site contains enough space for the proliferative cells to produce their offspring in their current location they will do so. (b) If the lattice site can not contain the new offspring then it will be created in the neighbouring site with the most available space. In the example the first two cells selected have enough space in their site to create their offspring. The remaining ones have to select a neighbouring site and since empty ones are preferred then each cell choses a different neighbouring site.

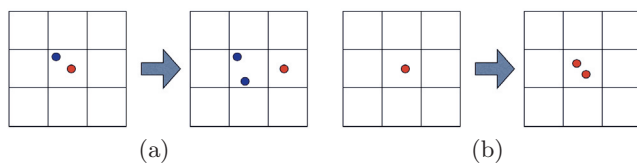


Fig. 3. Behaviour of motile cells. (a) In this example motile cells are red and proliferative cells are blue. If a motile cell is not alone in the lattice site then it will move to a neighbouring site with the smallest cell density. This will leave all the site resources to the proliferative cell. (b) On the other hand if it does not have to share the site with any other tumour cell then it will divide. In the following time step, at least one of them will have to move to a different location if there is any site with a lower cell count in the neighbourhood.

- move to new location if cell count is smaller than
in current location;
- Otherwise:
- if there is enough space in the current lattice site
then divide;
- else
 - look for the lattice site with the smallest number
of cells;
 - if chosen site has enough space produce off-
spring;
 - if offspring has been produced then, with a
small probability, mutate new cell to motile;

Every time step each of the tumour cells is chosen to have
 its programme executed. The order in which the cells are
 called is randomly selected in each time step to avoid po-
 tential biases. The simulations start with a group of proli-
 ferative cells placed in the centre of the lattice (circumfer-
 ence with radius 20 lattice sites). Every time proliferative
 cells divide there is a small chance (10^{-5}) that there will
 be a mutation conferring the offspring the motile pheno-
 type. Motile cells on the other hand will never produce
 proliferative cells when dividing. The reasoning for this is
 that the mutations in our model are not necessarily ge-
 netical but all have an effect on the phenotype. Whereas
 cells in tumour in an early stage of development tend to be

1 proliferative, the acquisition of motility and invasiveness
 2 is a necessary capability that may emerge as a result of a
 3 number of genetic and epigenetic mutations [2]. Hence, it
 4 is very unlikely that a motile cell could produce offspring
 5 that would accumulate the necessary mutations to disable
 6 this capability.

7 5 Simulations and analysis

8 The CA model was used to produce several simulations
 9 (e.g. Fig. 4), each one lasting 5000 timesteps, in which
 10 different values of nutrient replenishment and capacity of
 11 the lattice sites were tested.

12 Figure 5 shows the results of the simulations. The
 13 curves represent the proportion of motile cells that re-
 14 sults for values of nutrient replenishment between 1 and
 15 25. Each line represents a different lattice site carrying
 16 capacity of 10, 20, 50 and 100 cells per site.

17 The results from both analysis and simulations support
 18 current medical knowledge: if the cost of motility is zero
 19 then the motility phenotype will reach fixation and spread
 20 through the tumour population. If the cost of motility in-
 21 creases, so does the proportion of proliferative cells in the
 22 population. The proportion of motile cells in the simula-
 23 tions depends on the carrying capacity and the amount of
 24 nutrients. Simulations in which lattice sites can host many
 25 cells but nutrient availability is scarce, the cost of motility
 26 in relation to the cost of remaining in the same place is
 27 quite low and thus yield a high proportion of motile cells.
 28 On the other hand when lattice sites can carry just a few
 29 cells forcing proliferative cells to produce their offspring
 30 in neighbouring sites then the relative cost of motility in-
 31 creases and likewise the proportion of proliferative cells.

32 In the CA model the ratio of nutrients per lattice site
 33 capacity gives a measure of the cost of motility (c) rela-
 34 tive to the maximum fitness benefit (b). When the ratio of
 35 nutrients per lattice site capacity is high then the relative
 36 cost of motility will be high too. In these situations there
 37 are plenty of nutrients so that proliferative cells normally
 38 have enough resources to divide in every time step and
 39 thus out-compete motile cells. On the other hand if the
 40 ratio of nutrients per cell site is low then many prolifera-
 41 tive cells will not have enough nutrients and might have
 42 less opportunities to produce offspring than cells with the
 43 motile phenotype.

44 6 Conclusions

45 We have introduced a game theoretical model that al-
 46 lows the study of the emergence of invasion and motil-
 47 ity in tumours made of proliferative cells. We have also
 48 shown a CA model designed to study how spatial consid-
 49 erations could alter the results yielded by the GT analysis.
 50 The existence of polymorphic tumours has been found in
 51 other GT models [13] and the results from both, our GT
 52 analysis and the CA-based simulations, confirm that there
 53 are many circumstances under which different strategies

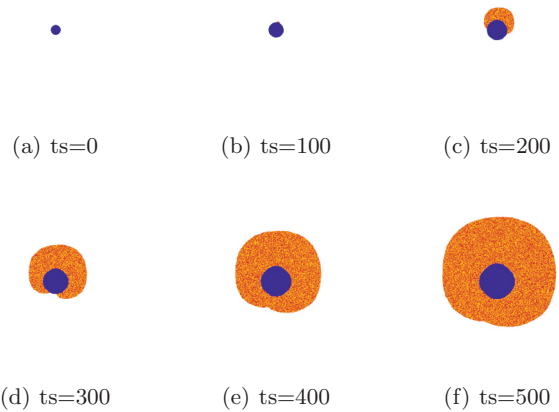


Fig. 4. Result of a sample simulation produced by the CA model. In this particular simulation each lattice site can host up to 10 tumour cells. Every time step only one unit of nutrients is replenished in each site. These circumstances reduce the cost of motility and thus select for the motile phenotype. Lattice sites which contain exclusively proliferative cells are marked in blue, those that contain only motile cells are red and finally those that contain more than one type of cell are orange.

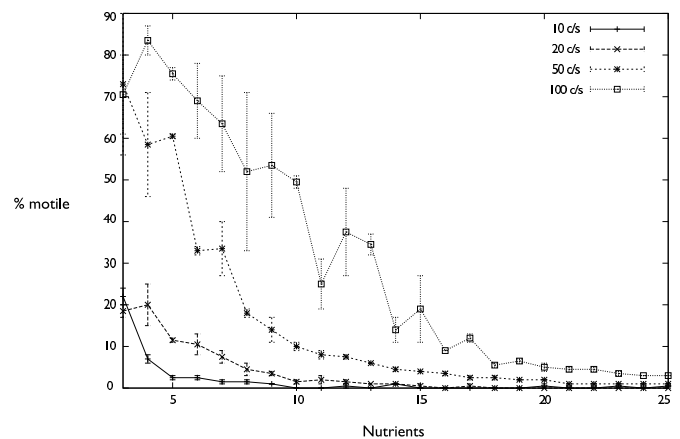


Fig. 5. The graph shows the proportion of motile cells (Y-axis) that result from using different amount of nutrients per time step (X-axis) after running the CA model for 500 time steps. The results are for different carrying capacities of each lattice site (10, 20, 50 and 100 cells/site). In all cases increasing the amount of nutrients supplied each time step reduces the proportion of motile tumour cells.

could be present in the tumour cell population at a given
 time. Many simplifications were made in order to get a
 model tractable enough to be simulated and analysed. It
 is clear that more than two phenotypes are possible at
 this stage of carcinogenesis and that tumour cells usually
 interact in a more complex fashion than the one used in
 this study. The microenvironment was also kept as simple
 as possible. It is clear that more complex microenviron-
 ments (with differences in the concentration of e.g. pH,
 oxygen, ECM and nutrients) should have an influence of
 the fitness of the two phenotypes. Many of these simplifica-

tions are necessary and similar to those adopted by other researchers [12–15,19]. This fact does not detract merit from the potential of the model to test the ideas behind the word models usually put forward by oncologists [2]. The simulations also support a therapy that would raise the cost of motility with respect to the base benefit to reduce the proportion of tumour cells capable of motility. Thus, by increasing the relative fitness advantage of non-motile phenotypes increases the probability of the tumour remaining benign. Increasing the cost of motility could be achieved in at least two different ways. One option would be to design therapies to hinder the detachment of tumour cells from the extra-cellular matrix by means of downregulation of integrins [37]. Alternatively, the model suggests the counter-intuitive idea that it should be possible to increase the fitness of proliferative cells over motile cells by increasing the amount of nutrients in the neighbourhood of the tumour. Increasing the amount of nutrients (Eq. (1)) produces the same effect as acting directly on the cost of motility. It seems reasonable to think that increasing the amount of nutrients would act as a disincentive for a tumour cell to become motile. This is not necessarily a therapy that would work in all cases: there are benign tumours that are life threatening even if they do not become invasive. Despite that, there are many cases in which a growing but non aggressive tumour will have a much better prognosis than a smaller but invasive one. In those cases this therapy could help the patient by producing a tumour environment that selects for less aggressive phenotypes.

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